# OPTIMAL DESCRIPTORS BASED ON EXTENDED CONNECTIVITY AND CODES OF CYLES: QSPR OF HYDROCARBON NORMAL BOILING POINTS 

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#### Abstract

: $(0,1)$-codes reflected presence / absence of six- and fivemembers cycles produce considerable improving statistical characteristics of quantitative structure-property relationships between optimal descriptors and normal boiling points of alkanes, alkylbenzenes, and polyaromatic hydrocarbons.


Keywords: QSPR, normal boiling points, hydrocarbons, cycle code, optimal descriptors

## INTRODUCTION

Our real world is rather uncertain. Suppose we are carrying out a chemical reaction, which allows us to obtain a product. In the very beginning we observe a complete uncertainty regarding the molecule. In fact, we have no information about its composition, the constitution of the molecular skeleton, its stereochemical features, its physical properties and biological activities and so on. Gradually, performing routine suitable experiments, we gather data. Then the acquisition of the structural information is complete there is no uncertainty, at least about its structure. The information about a real physical system is a measure of decreasing uncertainty of the system by means of some physical acitivities.

We can define knowledge as the perception of the logical relations among the structures of the information. Any systematic treatment of information needs some previous knowledge. Therefore, research is always an iterative process, as depicted in Scheme 1 [1].

## SCHEME 1



The central problem in theory of Quantitative Structure Property-Activity Relationships (QSPR/QSAR) is to convert chemical structures in to mathematical molecular descriptors that are relevant to the physico-chemical property or to the mechanism of the biological activity. Topological indices are among the best descriptors, although there are other sort of them, such as Molecular Orbital indices and other properties/activities which are also employed in these studies. It is a well known fact that molecular structure is one of the basic concepts of chemistry since properties and molecular behavior follow from their structures. In particular, properties of a molecule are a consequence of a complicated interplay of its topology (i.e. atomic connectivity), metric characteristics (bond lengths, valence and torsional angles) and detailed dynamics of electrons and nuclei. Finding out how various molecular features depend on molecular structure is one of the central fields of chemistry and particularly the main subject of QSAR/QSPR studies [2].

The topological indices are those structure molecular descriptors derived from a graph theoretical representation of molecules. These molecular descriptors should carry out most of the desired attributes for topological indices. Flexible topological descriptors make up a quite efficient set of variables to employ in QSAR/QSPR studies which have been employed successfully in many cases to predict physico-chemical properties and biological activities [310].

In a recent study [11] on the comparison of QSPR models based on hydrogen-filled graphs and on graphs of atomic orbitals, optimal descriptors have been calculated without taking into account the presence/absence of cycles in the molecular structure. The aim of the present study is to estimate the efficacy of codes of six- and five-member cycles in constructing optimal descriptors in order to get a better molecular description. We have chosen a set of 140 hydrocarbons to predict their normal boiling points.

## METHOD

Descriptors used in the present study have been calculated as
${ }^{1} \operatorname{DCW}\left(\mathrm{a}_{\mathrm{k}}, E C_{\mathrm{k}}\right)=\left\{\sum_{\mathrm{k}=1}^{\mathrm{n}} \operatorname{CW}\left(\mathrm{a}_{\mathrm{k}}\right)+\sum_{\mathrm{k}=1}^{\mathrm{n}} \operatorname{CW}\left({ }^{\mathrm{x}} \mathrm{EC}_{\mathrm{k}}\right)\right\}^{\mathrm{m}}$
${ }^{2} \operatorname{DCW}\left(\mathrm{a}_{\mathrm{k}}, \mathrm{EC}_{\mathrm{k}}\right)=\left\{\mathrm{CW}(\mathrm{CC})+\sum_{\mathrm{k}=1}^{\mathrm{n}} \mathrm{CW}\left(\mathrm{a}_{\mathrm{k}}\right)+\sum_{\mathrm{k}=1}^{\mathrm{n}} \mathrm{CW}\left({ }^{\mathrm{x}} \mathrm{EC}_{\mathrm{k}}\right)\right\}^{\mathrm{m}}$
where:
$\mathrm{a}_{\mathrm{k}}$ is chemical element (C or H ) in hydrogen-filled molecular graph (HFG) that is presented by k-th vertex in the graph,
${ }^{\mathrm{x}} \mathrm{EC}_{\mathrm{k}}$ is the extended connectivity of x -th order ( $\mathrm{x}=0,1,2$ ),
CC is the code of cycles, and they were calculated as shown in Table 1,
$\mathrm{CW}\left(\mathrm{a}_{\mathrm{k}}\right)$ is the correlation weight of presence $\mathrm{a}_{\mathrm{k}}$ in HFG, $\mathrm{CW}\left({ }^{\mathrm{X}} \mathrm{EC}_{\mathrm{k}}\right)$ is the correlation weight for a given extended connectivity value, $\mathrm{CW}(\mathrm{CC})$ is the correlation weight of the code of cycles, n is the number of vertex in the HFG, and $\mathrm{m}=0.5$.

Numerical data on the $\mathrm{CW}\left(\mathrm{a}_{\mathrm{k}}\right), \mathrm{CW}\left({ }^{\mathrm{x}} \mathrm{EC}_{\mathrm{k}}\right)$, and $\mathrm{CW}(\mathrm{CC})$ have been calculated via Monte Carlo optimization method, i.e., we look for those values of the CWs producing maximal correlation coefficient between ${ }^{9}$ DCW and normal boiling points (NBPs) of hydrocarbon of the training set have been obtained by the corresponding optimization procedure. From the data one can then calculate the desired physical chemistry property by the Least Square method NBP model
$\mathrm{NBP}=\mathrm{C}_{0}+\mathrm{C}_{1}{ }^{\mathrm{q}} \mathrm{DCW}\left(\mathrm{a}_{\mathrm{k}}, \mathrm{EC}_{\mathrm{k}}\right)$
Predictive potential of the model must be validated with an external test set. Recently these hydrocarbons have been examined in Ref. 11. We have resorted to the splitting of the whole molecular set into a training and a test set from the study. Choice of $\mathrm{m}=0.5$ is based on fact that often correlation between normal boiling points and descriptors are non linear $[12,13]$. We have tested $m=1$ and $m=0.5$. Statistical characteristics in case of $m=0.5$ were better than those corresponding to $\mathrm{m}=1$. Details on models with $\mathrm{m}=1$ will not be examined further in this paper. Calculation of the extended connectivity of increasing orders has been described in Ref. 14. Version of the Cycle codes (CC) are shown in Table 1 and it is a particular case of the generalized CC definition used in [15].

## RESULTS AND DISCUSSION

From Table 2 one can see that ${ }^{2}$ DCW modeling gives a model of normal boiling points of better statistical quality than ${ }^{1}$ DCW modeling. Correlation weights, obtained in three probes of the Monte Carlo optimization, for calculation of the ${ }^{2} \mathrm{DCW}$, are shown in Table 3. Calculation of the ${ }^{2} \operatorname{DCW}\left(\mathrm{a}_{\mathrm{k}},{ }^{1} \mathrm{EC}_{\mathrm{k}}\right)$ for m -xylene is shown in Table 4. The model of the hydrocarbon normal boiling points obtained in first probe of the optimization is the following
$\mathrm{NBP}=-448.8+117.52 *{ }^{2} \operatorname{DCW}\left(\mathrm{a}_{\mathrm{k}},{ }^{1} \mathrm{EC}_{\mathrm{k}}\right)$
$\mathrm{n}=70, \mathrm{r}^{2}=0.9988, \mathrm{~s}=5.86, \mathrm{~F}=57619$ (training set)
$\mathrm{n}=70, \mathrm{r}^{2}=0.9990, \mathrm{~s}=4.82, \mathrm{~F}=68071$ (test set)
The results derived from this model is displayed graphically for training and test sets in Figures 1 and 2, respectively. This model is slightly better than one described in [11], but the it is considerably simpler than the previous one.

## CONCLUSIONS

We have shown that utilization of the described cycle codes produce considerable improving statistical quality models of hydrocarbon normal boiling points regarding those calculation which do not take into account the presence of such cycles. In order to get a better conclusion on the goodness of the method proposed here, it is necessary to perform complementary calculations on other physicochemical properties and biological activities for other sets of molecules. Work along these lines are currently under development and results will be presented elsewhere in the forthcoming future.

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Table 1. Definition of the $(0,1)$ cycle codes $(C C)$.

| Situation in molecular structure | Numerical value of the CC |
| :--- | :---: |
| There is no cycle | C 00 |
| Six member cycle (one or more) | C 10 |
| Five member cycle (one or more) | C 01 |
| Both six-member and five-member cycles | C 11 |

Table 2. Statistical characteristics on the ${ }^{1}$ DCW- and ${ }^{2}$ DCW-modeling.

| Probe |  | $\mathbf{N o p}^{*}$ | $\mathrm{C}_{1}$ | $\mathrm{C}_{0}$ | $\mathbf{r}^{2}$ | s, ${ }^{0} \mathrm{C}$ | F | $\mathbf{r}^{2}$ | s, ${ }^{0} \mathrm{C}$ | F |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ${ }^{1}$ DCW-modeling |  |  |  |  |  |  |  |  |  |  |
| 1 | ${ }^{0} \mathrm{EC}$ | 5 | 50.759 | -378.100 | 0.9917 | 15.526 | 8140 | 0.9935 | 12.595 | 10351 |
| 2 |  |  | 56.014 | -378.098 | 0.9917 | 15.526 | 8140 | 0.9935 | 12.596 | 10351 |
| 3 |  |  | 53.229 | -378.123 | 0.9917 | 15.526 | 8140 | 0.9935 | 12.595 | 10353 |
| 1 | ${ }^{1} \mathrm{EC}$ | 10 | 79.442 | -364.654 | 0.9958 | 11.065 | 16092 | 0.9958 | 9.874 | 16260 |
| 2 |  |  | 86.660 | -364.808 | 0.9958 | 11.065 | 16092 | 0.9958 | 9.874 | 16262 |
| 3 |  |  | 81.802 | -364.789 | 0.9958 | 11.065 | 16092 | 0.9958 | 9.877 | 16252 |
| 1 | ${ }^{2} \mathrm{EC}$ | 23 | 113.195 | -497.071 | 0.9991 | 5.207 | 72900 | 0.9959 | 9.735 | 16488 |
| 2 |  |  | 118.798 | -497.180 | 0.9991 | 5.208 | 72893 | 0.9959 | 9.742 | 16467 |
| 3 |  |  | 116.924 | -495.901 | 0.9991 | 5.210 | 72830 | 0.9959 | 9.690 | 16642 |

${ }^{2}$ DCW-modeling

| 1 | ${ }^{0}$ EC | 8 | 153.759 | -656.597 | 0.9979 | 7.818 | 32303 | 0.9980 | 6.893 | 33635 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 |  |  | 149.916 | -635.847 | 0.9979 | 7.834 | 32177 | 0.9980 | 6.911 | 33477 |
| 3 |  |  | 153.089 | -661.713 | 0.9979 | 7.815 | 32331 | 0.9980 | 6.896 | 33603 |
| $\mathbf{1}$ | ${ }^{1}$ EC | $\mathbf{1 3}$ | $\mathbf{1 1 7 . 5 2 6}$ | $\mathbf{- 4 4 8 . 8 0 5}$ | $\mathbf{0 . 9 9 8 8}$ | $\mathbf{5 . 8 5 7}$ | $\mathbf{5 7 6 1 9}$ | $\mathbf{0 . 9 9 9 0}$ | $\mathbf{4 . 8 2 1}$ | $\mathbf{6 8 0 7 1}$ |
| $\mathbf{2}$ |  |  | $\mathbf{1 1 9 . 4 0 0}$ | $\mathbf{- 4 4 2 . 5 3 3}$ | $\mathbf{0 . 9 9 8 8}$ | $\mathbf{5 . 8 6 6}$ | $\mathbf{5 7 4 3 4}$ | $\mathbf{0 . 9 9 9 0}$ | $\mathbf{4 . 8 3 0}$ | $\mathbf{6 7 7 4 4}$ |
| $\mathbf{3}$ |  |  | $\mathbf{1 1 0 . 4 8 1}$ | $\mathbf{- 4 3 8 . 2 2 5}$ | $\mathbf{0 . 9 9 8 8}$ | $\mathbf{5 . 8 7 1}$ | $\mathbf{5 7 3 3 2}$ | $\mathbf{0 . 9 9 9 0}$ | $\mathbf{4 . 8 2 5}$ | $\mathbf{6 7 8 6 8}$ |
| 1 | ${ }^{2}$ EC | 26 | 115.581 | -537.107 | 0.9992 | 4.725 | 88550 | 0.9970 | 8.277 | 22824 |
| 2 |  |  | 108.701 | -534.546 | 0.9992 | 4.735 | 88180 | 0.9973 | 7.965 | 24661 |
| 3 |  |  | 113.946 | -534.428 | 0.9992 | 4.724 | 88599 | 0.9972 | 8.107 | 23802 |

${ }^{*}{ }^{*} \mathbf{N}_{\text {op }}$ is number of optimized parameters.

Table 3. Correlation weights for calculation ${ }^{2} \mathrm{DCW}\left(\mathrm{a}_{\mathrm{k}},{ }^{1} \mathrm{EC}_{\mathrm{k}}\right)$.

| HFG invaraint | CWs on probe 1 | CWs on probe 2 | CWs on probe 3 |
| :--- | :--- | :--- | :--- |
| Chemical elements, $\mathbf{a}_{\mathbf{k}}$ |  |  |  |
| H | 0.03124 | 0.17661 | 0.02428 |
| C | 0.00000 | 0.00000 | 0.00000 |
| Extended connectivity <br> of first order, ${ }^{1}$ EC $_{\mathbf{k}}$ |  |  |  |
| 0003 | 2.46163 | 2.24314 | 0.78192 |
| 0004 | 0.26443 | 0.12287 | 2.32249 |
| 0006 | 2.45652 | 2.36583 | 0.00068 |
| 0007 | 0.02004 | 0.00309 | 4.09422 |
| 0009 | 3.66781 | 3.52048 | 1.89861 |
| 0010 | 1.75035 | 1.64111 | 3.30193 |
| 0013 | 3.03027 | 2.84582 | 4.71470 |
| 0016 | 4.32879 | 4.07044 |  |
| $(0,1)$ cycle codes, CC |  |  | 8.19960 |
| C00 | 7.83707 | 7.22255 | 4.78143 |
| C10 | 4.86283 | 4.29464 | 2.51194 |
| C11 | 2.84091 | 2.35837 |  |

Table 4. Calculation of the ${ }^{2} \operatorname{DCW}\left(\mathrm{a}_{\mathrm{k}},{ }^{1} \mathrm{EC}_{\mathrm{k}}\right)$ for m-xylene.

$\mathrm{CW}(\mathrm{CC})=\mathrm{CW}(\mathrm{C} 10)=4.86283$
$\mathrm{CW}(\mathrm{CC})+\sum_{\mathrm{k}=1}^{\mathrm{n}} \mathrm{CW}\left(\mathrm{a}_{\mathrm{k}}\right)+\sum_{\mathrm{k}=1}^{\mathrm{n}} \mathrm{CW}\left({ }^{\mathrm{x}} \mathrm{EC}_{\mathrm{k}}\right)=25.10227$
$25.20227^{0.5}=5.01022$

| No. | $\mathbf{a}_{\mathbf{k}}$ | ${ }^{\mathbf{1}} \mathbf{E C}_{\mathbf{k}}$ | $\mathbf{C W ( \mathbf { a } _ { \mathbf { k } } )}$ | $\mathbf{C W}\left({ }^{\mathbf{1}} \mathbf{E C}_{\mathbf{k}}\right)$ |
| :---: | :--- | :---: | :---: | :---: |
| 1 | C | 10 | 0.00000 | 1.75035 |
| 2 | C | 7 | 0.00000 | 0.02004 |
| 3 | C | 10 | 0.00000 | 1.75035 |
| 4 | C | 7 | 0.00000 | 0.02004 |
| 5 | C | 7 | 0.00000 | 0.02004 |
| 6 | C | 7 | 0.00000 | 0.02004 |
| 7 | H | 3 | 0.03124 | 2.46163 |
| 8 | H | 3 | 0.03124 | 2.46163 |
| 9 | H | 3 | 0.03124 | 2.46163 |
| 10 | H | 3 | 0.03124 | 2.46163 |
| 11 | C | 6 | 0.00000 | 2.45652 |
| 12 | H | 4 | 0.03124 | 0.26443 |
| 13 | H | 4 | 0.03124 | 0.26443 |
| 14 | H | 4 | 0.03124 | 0.26443 |
| 15 | C | 6 | 0.00000 | 2.45652 |
| 16 | H | 4 | 0.03124 | 0.26443 |
| 17 | H | 4 | 0.03124 | 0.26443 |
| 18 | H | 4 | 0.03124 | 0.26443 |

Table 5. Experimental and calculated with Eq. (4) values of hydrocarbon normal boiling points on training and test sets.

| No. | Structures | DCW | NBP $_{\text {expr }}$ | $\mathbf{N B P}_{\text {cacl }}$ | $\mathrm{NBP}_{\text {expr }}-$ NBP $_{\text {calc }}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Training set |  |  |  |  |
| 1 | Ethane | 3.10664 | -88.60000 | -83.70767 | -4.89233 |
| 2 | Propane | 3.46307 | -42.10000 | -41.82001 | -0.27999 |
| 3 | 2,2-Dimethylpropane | 3.97418 | 9.50000 | 18.24563 | -8.74563 |
| 4 | 2-Methylbutane | 4.02814 | 27.80000 | 24.58701 | 3.21299 |
| 5 | 2-Methylpropane | 3.72615 | -11.70000 | -10.90285 | -0.79715 |
| 6 | n-Butane | 3.78610 | -0.50000 | -3.85753 | 3.35753 |
| 7 | 3-Methylpentane | 4.30901 | 63.30000 | 57.59486 | 5.70514 |
| 8 | n -Hexane | 4.36096 | 68.70000 | 63.70002 | 4.99998 |
| 9 | 3,3-Dimethylpentane | 4.52521 | 86.10000 | 83.00268 | 3.09732 |
| 10 | 2,3-Dimethylpentane | 4.52315 | 89.80000 | 82.76059 | 7.03941 |
| 11 | 3-Methylhexane | 4.57267 | 91.80000 | 88.58018 | 3.21982 |
| 12 | 3-Ethylpentane | 4.57267 | 93.50000 | 88.58018 | 4.91982 |
| 13 | 2,2,3-Trimethylpentane | 4.72957 | 109.80000 | 107.01907 | 2.78093 |
| 14 | 2,3,3-Trimethylpentane | 4.72957 | 114.80000 | 107.01907 | 7.78093 |
| 15 | 3,3-Dimethylhexane | 4.77694 | 112.00000 | 112.58599 | -0.58599 |
| 16 | 3-Ethyl-3-methylpentane | 4.77694 | 118.30000 | 112.58599 | 5.71401 |
| 17 | 3-Ethyl-2-methylpentane | 4.77500 | 115.60000 | 112.35800 | 3.24200 |
| 18 | 2,2-Dimethylbutane | 4.25861 | 49.70000 | 51.67185 | -1.97185 |
| 19 | 2,2,3,3-Tetramethylpentane | 4.92734 | 140.30000 | 130.26100 | 10.03900 |
| 20 | 2,2,3,4-Tetramethylpentane | 4.92545 | 133.00000 | 130.03888 | 2.96112 |
| 21 | 2,3,3-Trimethylhexane | 4.97097 | 137.70000 | 135.38839 | 2.31161 |
| 22 | 2,2,4,4-Tetramethylpentane | 4.92734 | 122.30000 | 130.26100 | -7.96100 |
| 23 | 2,2,4-Trimethylhexane | 4.97097 | 126.50000 | 135.38839 | -8.88839 |
| 24 | 2,4,4-Trimethylhexane | 4.97097 | 130.60000 | 135.38839 | -4.78839 |
| 25 | 3,3-Diethylpentane | 5.01606 | 146.20000 | 140.68737 | 5.51263 |
| 26 | 2,4-dimethyl-3-ethylpentane | 4.96909 | 136.70000 | 135.16746 | 1.53254 |
| 27 | 3-Ethyl-4-methylhexane | 5.01421 | 140.40000 | 140.46996 | -0.06996 |
| 28 | 4-Ethyl-2-methylhexane | 5.01421 | 133.80000 | 140.46996 | -6.66996 |
| 29 | 2-Methyloctane | 5.05892 | 143.30000 | 145.72428 | -2.42428 |
| 30 | 3-Methyloctane | 5.05892 | 144.20000 | 145.72428 | -1.52428 |
| 31 | 4-Ethylheptane | 5.05892 | 141.20000 | 145.72428 | -4.52428 |
| 32 | 2,2-Dimethylheptane | 5.01606 | 132.70000 | 140.68737 | -7.98737 |
| 33 | 2,5-Dimethylheptane | 5.01421 | 136.00000 | 140.46996 | -4.46996 |
| 34 | 2,6-Dimethylheptane | 5.01421 | 135.20000 | 140.46996 | -5.26996 |
| 35 | 3,5-Dimethylheptane | 5.01421 | 136.00000 | 140.46996 | -4.46996 |
| 36 | 3-Methyl-3-ethylhexane | 5.01606 | 140.60000 | 140.68737 | -0.08737 |
| 37 | Benzene | 4.46546 | 80.10000 | 75.98086 | 4.11914 |
| 38 | Toluene | 4.74566 | 110.60000 | 108.90996 | 1.69004 |
| 39 | m-Xylene | 5.01022 | 139.10000 | 140.00105 | -0.90105 |
| 40 | p-Xylene | 5.01022 | 138.40000 | 140.00105 | -1.60105 |
| 41 | 1-Methyl-3-ethylbenzene | 5.18892 | 161.30000 | 161.00188 | 0.29812 |
| 42 | 1-Methyl-4-ethylbenzene | 5.18892 | 162.00000 | 161.00188 | 0.99812 |
| 43 | 1,3,5-Trimethylbenzene | 5.26149 | 164.70000 | 169.53030 | -4.83030 |
| 44 | 1,2,3,4-Tetramethylbenzene | 5.50129 | 205.00000 | 197.71160 | 7.28840 |
| 45 | 1,3-Diethylbenzene | 5.36168 | 181.10000 | 181.30463 | -0.20463 |
| 46 | 1,4-Diethylbenzene | 5.36168 | 183.80000 | 181.30463 | 2.49537 |
| 47 | 1-Methyl-4-n-propylbenzene | 5.40986 | 183.80000 | 186.96675 | -3.16675 |
| 48 | 1,2-Dimethyl-3-ethylbenzene | 5.43194 | 193.90000 | 189.56159 | 4.33841 |
| 49 | 1,3-Dimethyl-4-ethylbenzene | 5.43194 | 188.40000 | 189.56159 | -1.16159 |
| 50 | 1,3-Dimethyl-5-ethylbenzene | 5.43194 | 183.80000 | 189.56159 | -5.76159 |
| 51 | 1,2,4,5-Tetramethylbezene | 5.50129 | 196.80000 | 197.71160 | -0.91160 |
| 52 | Naphthalene | 5.68346 | 218.00000 | 219.12022 | -1.12022 |
| 53 | Acenaphthylene | 6.13314 | 270.00000 | 271.96661 | -1.96661 |
| 54 | Acenaphthene | 6.10516 | 279.00000 | 268.67840 | 10.32160 |


| 55 | Fluoranthene | 7.06943 | 383.00000 | 381.99941 | 1.00059 |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 56 | Pyrene | 7.21102 | 393.00000 | 398.63907 | -5.63907 |
| 57 | Benzo(c)fluorene | 7.24498 | 406.00000 | 402.63005 | 3.36995 |
| 58 | Benzo(ghi)fluoranthene | 7.57050 | 422.00000 | 440.88516 | -18.88516 |
| 59 | Benz(a)anthracene | 7.55147 | 425.00000 | 438.64875 | -13.64875 |
| 60 | Dibenz(a,j)anthracene | 8.32983 | 531.00000 | 530.12162 | 0.87838 |
| 61 | Cyclopenta(cd)pyrene | 7.54785 | 439.00000 | 438.22333 | 0.77667 |
| 62 | Benzo(k)fluoranthene | 7.89546 | 481.00000 | 479.07446 | 1.92554 |
| 63 | Perylene | 8.02248 | 497.00000 | 494.00185 | 2.99815 |
| 64 | Anthanthrene | 8.46734 | 547.00000 | 546.28180 | 0.71820 |
| 65 | Indeno(1,2,3-cd)pyrene | 8.34709 | 534.00000 | 532.15002 | 1.84998 |
| 66 | Dibenz(a,c)anthracene | 8.32983 | 535.00000 | 530.12162 | 4.87838 |
| 67 | Picene | 8.32983 | 519.00000 | 530.12162 | -11.12162 |
| 68 | Coronene | 8.88997 | 590.00000 | 595.94927 | -5.94927 |
| 69 | Dibenzo(a,i)pyrene | 8.75909 | 594.00000 | 580.56826 | 13.43174 |
| 70 | Dibenzo(a,l)pyrene | 8.75909 | 595.00000 | 580.56826 | 14.43174 |
|  | Test set |  |  |  |  |
| 1 | 4-Methylheptane | 4.82193 | 117.70000 | 117.87321 | -0.17321 |
| 2 | n-Pentane | 4.08366 | 36.10000 | 31.11172 | 4.98828 |
| 3 | Dibenzo(a,e)pyrene | 8.75909 | 592.00000 | 580.56826 | 11.43174 |
| 4 | Dibenzo(a,h)pyrene | 8.75909 | 596.00000 | 580.56826 | 15.43174 |
| 5 | Dibenz(a,h)anthracene | 8.32983 | 535.00000 | 530.12162 | 4.87838 |
| 6 | Benzo(ghi)perylene | 8.46734 | 542.00000 | 546.28180 | -4.28180 |
| 7 | Indeno(1,2,3-cd)fluoranthene | 8.34709 | 531.00000 | 532.15002 | -1.15002 |
| 8 | Benz(a)pyrene | 8.02248 | 496.00000 | 494.00185 | 1.99815 |
| 9 | Benzo(e)pyrene | 8.02248 | 493.00000 | 494.00185 | -1.00185 |
| 10 | Naphthacene | 7.55147 | 440.00000 | 438.64875 | 1.35125 |
| 11 | Triphenylene | 7.55147 | 429.00000 | 438.64875 | -9.64875 |
| 12 | Benzo(b)fluoranthene | 7.89546 | 481.00000 | 479.07446 | 1.92554 |
| 13 | Chrysene | 7.55147 | 431.00000 | 438.64875 | -7.64875 |
| 14 | Benzo(a)fluorene | 7.24498 | 403.00000 | 402.63005 | 0.36995 |
| 15 | Benzo(b)fluorene | 7.24498 | 398.00000 | 402.63005 | -4.63005 |
| 16 | Fluorene | 6.33469 | 294.00000 | 295.65277 | -1.65277 |
| 17 | 4H-Cyclopenta(def)phenanthrene | 6.88941 | 359.00000 | 360.84346 | -1.84346 |
| 18 | Benzo(j)fluoranthene | 7.89546 | 480.00000 | 479.07446 | 0.92554 |
| 19 | Phenanthrene | 6.68305 | 338.00000 | 336.59204 | 1.40796 |
| 20 | Anthracene | 6.68305 | 340.00000 | 336.59204 | 3.40796 |
| 21 | 1,4-Dimethyl-2-ethylbenzene | 5.43194 | 186.90000 | 189.56159 | -2.66159 |
| 22 | 1,2,3,5-Tetramethylbenzene | 5.50129 | 198.20000 | 197.71160 | 0.48840 |
| 23 | 1,2-Dimethyl-4-ethylbenzene | 5.43194 | 189.80000 | 189.56159 | 0.23841 |
| 24 | 1,3-Dimethyl-2-ethylbenzene | 5.43194 | 190.00000 | 189.56159 | 0.43841 |
| 25 | 1-Methyl-2-n-propylbenzene | 5.40986 | 184.80000 | 186.96675 | -2.16675 |
| 26 | 1-Methyl-3-n-propylbenzene | 5.40986 | 181.80000 | 186.96675 | -5.16675 |
| 27 | n-Butylbenzene | 5.38770 | 183.30000 | 184.36250 | -1.06250 |
| 28 | 1,2-Diethylbenzene | 5.36168 | 183.40000 | 181.30463 | 2.09537 |
| 29 | 1,2,3-Trimethylbenzene | 5.26149 | 176.10000 | 169.53030 | 6.56970 |
| 30 | 1,2,4-Trimethylbenzene | 5.26149 | 169.40000 | 169.53030 | -0.13030 |
| 31 | n-Propylbenzene | 5.16582 | 159.20000 | 158.28717 | 0.91283 |
| 32 | 1-Methyl-2-ethylbenzene | 5.18892 | 165.20000 | 161.00188 | 4.19812 |
| 33 | Ethylbenzene | 4.93396 | 136.20000 | 131.03898 | 5.16102 |
| 34 | o-Xylene | 5.01022 | 144.40000 | 140.00105 | 4.39895 |
| 35 | 3,3,4-Trimethylhexane | 4.97097 | 140.50000 | 135.38839 | 5.11161 |
| 36 | 2,3,4-Trimethylhexane | 4.96909 | 139.00000 | 135.16746 | 3.83254 |
| 37 | 3,3-Dimethylheptane | 5.01606 | 137.30000 | 140.68737 | -3.38737 |
| 38 | 3,4-Dimethylheptane | 5.01421 | 140.60000 | 140.46996 | 0.13004 |
| 39 | 2,3-Dimethylheptane | 5.01421 | 140.50000 | 140.46996 | 0.03004 |
| 40 | 2,4-Dimethylheptane | 5.01421 | 133.50000 | 140.46996 | -6.96996 |
| 41 | 4-Methyloctane | 5.05892 | 142.50000 | 145.72428 | -3.22428 |
| 42 | 3-Ethylheptane | 5.05892 | 143.00000 | 145.72428 | -2.72428 |


| 43 | 3,4-Dimethylhexane | 4.77500 | 117.70000 | 112.35800 | 5.34200 |
| :---: | :--- | :---: | :---: | :---: | :---: |
| 44 | n-Nonane | 5.10324 | 150.80000 | 150.93276 | -0.13276 |
| 45 | 2,3,5-Trimethylhexane | 4.96909 | 131.30000 | 135.16746 | -3.86746 |
| 46 | 3-ethyl-2-methyl-hexane | 5.01421 | 138.00000 | 140.46996 | -2.46996 |
| 47 | 2,2,5-Trimethylhexane | 4.97097 | 124.10000 | 135.38839 | -11.28839 |
| 48 | 4,4-Dimethylheptane | 5.01606 | 135.20000 | 140.68737 | -5.48737 |
| 49 | 2,3-dimethyl-3-ethylpentane | 4.97097 | 142.00000 | 135.38839 | 6.61161 |
| 50 | 2,2,3-Trimethylhexane | 4.97097 | 133.60000 | 135.38839 | -1.78839 |
| 51 | 2,2-dimethyl-3-ethylpentane | 4.97097 | 133.80000 | 135.38839 | -1.58839 |
| 52 | 2,3,3,4-Tetramethylpentane | 4.92545 | 141.60000 | 130.03888 | 11.56112 |
| 53 | 3-Ethylhexane | 4.82193 | 118.50000 | 117.87321 | 0.62679 |
| 54 | n-Octane | 4.86841 | 125.70000 | 123.33554 | 2.36446 |
| 55 | 2,5-Dimethylhexane | 4.77500 | 109.10000 | 112.35800 | -3.25800 |
| 56 | 2-Methylheptane | 4.82193 | 117.60000 | 117.87321 | -0.27321 |
| 57 | 2,3,4-Trimethylpentane | 4.72760 | 113.50000 | 106.78755 | 6.71245 |
| 58 | 2,3-Dimethylhexane | 4.77500 | 115.60000 | 112.35800 | 3.24200 |
| 59 | 2,2,4-Trimethylpentane | 4.72957 | 99.20000 | 107.01907 | -7.81907 |
| 60 | 2,2-Dimethylhexane | 4.62165 | 98.40000 | 94.33631 | -5.78599 |
| 61 | n-Heptane | 4.68370 | 106.50000 | 101.62842 | 4.06369 |
| 62 | 2,2,3,3-tetramethylbutane | 4.52315 | 80.50000 | 82.76059 | -2.26059 |
| 63 | 2,4-Dimethylpentane | 4.57267 | 90.00000 | 88.58018 | 1.41982 |
| 64 | 2-Methylhexane | 4.47516 | 80.90000 | 77.12080 | 3.77920 |
| 65 | 2,2,3-Trimethylbutane | 4.52521 | 79.20000 | 83.00268 | -3.80268 |
| 66 | 2,2-Dimethylpentane | 4.25643 | 58.00000 | 51.41565 | 6.58435 |
| 67 | 2,3-Dimethylbutane | 4.30901 | 60.30000 | 57.59486 | 2.70514 |
| 68 | 2-methylpentane | 4.77500 | 109.40000 | 112.35800 | -2.95800 |
| 69 | 2,4-Dimethylhexane | 4.82193 | 118.90000 | 117.87321 | 1.02679 |
| 70 | 3-Methylheptane |  |  |  |  |



Figure 1. Plot of experimental vs. calculated with Eq. (4) normal boiling points on the training set.


Figure 2. Plot of experimental vs. calculated with Eq. (4) normal boiling points on the test set.

